oxidize the purple solution to a colorless solution. Zinc amalgam spirals reduced the colorless solution back to a purple solution.

Dissolution of titanium in hydrofluoric acid in Pyrex test-tubes proceeds at a moderate rate to produce a purple solution. This reaction moderates, then proceeds vigorously to a green solution which is more stable to air than the purple, but also yields a colorless solution when in contact with oxygen, permanganate or ceric ions. The green solution is regenerated by placing zinc anialgam spirals in the colorless solution. Moreover, simply pouring some

of the purple solution (from the polyethylene bottle) into a Pyrex test-tube produces the green solution. Quantitative oxidations with ceric ions show that both the green and purple solutions contain trivalent titanium while the colorless solutions contain tetravalent titanium. It appears that the green solution is a titanium-silicon-fluoride complex.

Acknowledgment—The authors wish to thank the Research Corporation for financial assistance.

WACO, TEXAS

[CONTRIBUTION FROM THE	DEPARTMENT	ог Сн	emistry, Anti	OCH COLLEGE
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Hydrothermal Reactions in the Na₂O-GeO₂ System¹

BY ELWOOD R. SHAW, JAMES F. CORWIN AND JAMES W. EDWARDS

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The hydrothermal reactions between GeO_2 and water and water solutions containing sodium hydroxide have been studied at temperatures between 100 and 400°, and in the time range from 1 to 384 hours. The reaction of GeO_2 with water resulted in no new crystalline forms, but with solutions containing sodium hydroxide two crystalline forms having the proposed formulas $Na_3HGe_7O_{16}4H_2O$ and $Na_2Ge_4O_9$ were prepared in such quantity that optical recognition and properties were easily established. The anhydrous material has heretofore been prepared by ignition only. On the basis of chemical analysis and pH determination mechanisms for the formation of these crystals are proposed.

Introduction

The early work^{2,3} in the Na₂O-GeO₂ system consisted of studies of the melting point diagrams of mixtures. Eutectics were found at Na₂O-GeO₂ ratios of 1:1, 1:2 and 1:4 corresponding to compounds with the general formulas Na2GeO3, Na2-Ge₂O₅ and Na₂Ge₄O₉, respectively. The metagermanate and the tetragermanate have been prepared, but only the hydrated metagermanate has been characterized in the literature.4-7

Our studies of the products of hydrothermal reactions of NaOH-GeO2 mixtures have shown that a condensed, anhydrous sodium germanate can be prepared in three crystalline habits and occurs as a single phase in the products of the reaction. Thus, the compound can be physically characterized and the structure determined.⁸ By varying the conditions of the reaction the sodium hydrogen germanate described earlier by Nowotny and Wittinann⁶ has been prepared in crystals of somewhat less regular habit. This hydrogen germanate is shown by X-ray studies to be the same compound precipitated at room temperatures from NaOH-GeO2 mixtures containing NaCl. Infrared studies have shown the compound to be a definite hydrate so that the formula Na₃HGe₇O₁₆·4H₂O⁶ is confirmed as preferable to Na₂Ge₅O₁₁.^{9,10}

(1) This research was supported by the United States Air Force through the Air Force Office of Scientific Research of the Air Research and Development Command, under contract No. AF 18(600)1490. Reproduction in whole or in part is permitted for any purpose of the United States Government.

(2) R. Schwarz and M. Lewinsohn, Ber., 63, 783 (1930).

(3) R. Schwarz and F. Heinrich, Z. anorg. allgem. Chem., 205, 43 (1932).

(4) O. Johnson, Chem. Revs., 51, 421 (1952).

(5) H. Nowotny and A. Wittmann, Monatsh., 84, 701 (1953).

(6) H. Nowotny and A. Wittmann, ibid., 85, 558 (1954).

(7) A. Wittmann and H. Nowotny, ibid., 87, 654 (1956).

(8) This work is being readied for publication by Dr. John F. White, Department of Geology, Antioch College.

Ignition of this sodium hydrogen germanate at 900° caused a loss of 10.6% water and produced a compound with an identical X-ray pattern to that of the condensed anhydrous germanate synthesized hydrothermally from NaOH-GeO2 mixtures and to that of a compound formed when a Na₂CO₃-GeO2 mixture in the molar ratio 1:4 was fused at 900°.

From somewhat parallel reactions described by Nowotny and Wittmann,⁶ and on the basis of Na₂O -GeO2 analysis, the condensed germanate is identified as sodium tetragermanate.

By a similar hydrothermal reaction the ammonium and potassium hydrogen germanates were prepared; however the methods used for the hydrothermal conversion of sodium hydrogen germanate to the corresponding tetragermanate had no effect on the ammonium compound.

Hydrothermal runs in the GeO_2-H_2O system for purposes of familiarization with the products for optical identification confirmed the work of Laubengayer and Morton¹¹; however new indices of refraction are proposed for the soluble form. Also, runs which were quenched produced birefringent, fibrous crystals with an average index of 1.66, close to that found for the commercial¹² GeO₂, 1.64-1.65, and to that reported in a handbook¹³ for GeO_2 , 1.65.

Experimental

Reagents.—Reagent grade chemicals were used in all cases unless otherwise described below. The germanium dioxide12 was either in the form of a microcrystalline powder, 99.99% pure, or a fused glass in chunks of 5 mm. or less in

(9) D. Everest and J. Salmon, J. Chem. Soc., 2438 (1954).

(10) G. Carpeni, J. chim. phys., 45, 130 (1948).

(11) A. Laubengayer and D. Morton, THIS JOURNAL, 54, 2303 (1932).

(12) A. D. Mackay, Inc., New York, N. Y.
(13) N. Lange, "Handbook of Chemistry," Handbook Pub., Inc., Sandusky, Ohio, 1952.

diameter. All solutions or mixtures were made using distilled, demineralized water and were stored in stoppered polyethylene bottles. Acidic solutions only were allowed to remain in glassware for more than 0.5 minute except during centrifugation when the high GeO₂ and Na₂O content minimized the effect of any possible contamination. Silica-free NH₃ water was prepared by bubbling NH₃ through distilled water in a polyethylene container. This solution or dilute H₂SO₄ was used in *p*H adjustments during analysis. Equipment and Procedure.—Hydrothermal runs were

Equipment and Procedure.—Hydrothermal runs were made in 10-ml. stainless steel autoclaves with wedge caps held down by screw caps. Germanium dioxide analyses were run colorimetrically on a Beckman DU spectrophotometer. This method was checked on each type of sample by use of the gravimetric procedure of Hecht and Bartelnus.¹⁴

The sodium analyses were performed using a Weichselbaum-Varney Flame Photometer with sodium chloride standards.

Water was determined gravimetrically by ignition of samples to 900° after drying at 110°. No appreciable water was detected by infrared analysis in samples shown by gravimetric procedures to be anhydrous.

In the exploratory runs analytical control was not attempted. Two NaOH-GeO₂ mixtures were prepared in which the pH was adjusted to 10.4 with enough excess GeO₂ to precipitate solid material. The first mixture, which drifted to pH 7.8 and became gelatinous in five months, was found by later analysis to have a GeO₂/Na₂O molar ratio of 3.8. The second mixture drifted to pH 9.7 in several months and was found to contain a GeO₂/Na₂O molar ratio of 3.3.

A series of quantitative reactions also was run. The ratio of Na_2O/GeO_2 was held constant and the time of run varied. The resulting solutions and solids were analyzed to determine the molar ratio of GeO_2/Na_2O . A constant ratio was taken to indicate that equilibrium had been reached between the solution and solid phases.

Results

Tables I and II show the results of the reaction of NaOH–GeO₂ mixtures at 12 atmospheres pressure. In each case an attempt has been made in the tables to equate the optical description with the phases detected by X-ray methods. To check

TABLE I

REACTIONS OF pH 7.8 NaOH-GeO2 MIXTURE AT 200°

hr.	Final ⊅H	Optica	X-ray	
	-	Crystals	Index	
2	7.6	Octagonal prisms	1,690,1.695	Unknown I only
2^a	6.5	Cubes ^b	1.695, 1.72	Soluble form
		Oct. prisms	1.690, 1.695	Unknown I
				Unknown II
2^{c}	8.0	Rectangular solids	1,690,1.695	Strong-unk. 1
		Irregular crystals		
		(Isotropic)	1,63-1,64	Medium
				NH4H2Ge2O6 ^d
43	7.9	Rect. solids	1.690, 1.695	Unknown I only
2	7.9	Rect. solids	1.690, 1.695	Strong, unk. I
		Irregular crystals	1.63-1.64	Faint
				$NH_4H_3Ge_2O_6$
		Twinned crystals ^e		Weak-unk, II

^a GeO₂ glass was added to this run. ^b Exhibit diagonal extinction. ^c Quenched in cold water. ^d Obviously the sodium salt; however only ammonium pattern is available. ^e The twinned crystals extinguish diagonally. Top indices 1.690, 1.695; side 1.695, 1.72.

the possibility that Unknown II was the other form of Na₂Ge₄O₉ reported by Nowotny and Wittmann⁶ some of Unknown I and also a 1:4 Na₂CO₃–GeO₂ mixture were fused at 1054° and cooled slowly. A crystalline compound with the indices of refraction $N_0 = 1.740$, $N_E = 1.76$ –1.77 resulted as a single phase in each case. Analysis by X-ray methods indicated that no detectible amount of

(14) F. Hecht and G. Bartelmus, Mikrochem., 36/37, 466 (1950).

any previously prepared germanate was present. The infrared pattern resembled somewhat that for the tetragermanate; however, there were additional bands not present in any other pattern. Identification of this form is in progress.

TABLE II

REACTIONS OF pH 9.7 NaOH-GeO2 MIXTURE

Time, temp.	Final ⊅H	Analysis			
-		Optical	X-Ray		
2 hr.	9.5	Isotropic crystals	1.63 - 1.64	(S) NH4H3Ge2O8ª	
200°					
8 da.	11.8	Large dipyramids	1.690, 1.695	(S) Unknown I	
200		(40-50 microns)			
12 da.^{b}	10.2	Small dipyramids	1.690, 1.695	(S) Unknown I	
200		(10–14 microns)			
26 da.	9. 8	Isotropic crystals	1.63-1.64	Note e	
110		Very small crystals ^d	(birefringent)		
13 da.	11.2	Same as at 110°			

150 Many more birefringent crystals.

^a See note (d) Table I; (S) = strong. ^b Germanium dioxide glass added. ^c Infrared analysis gave same pattern as 200°-hr. run. ^d Very few—not detected on infrared pattern. ^e X-Ray analysis indicates a mixture of two $MH_3Ge_2O_6$, (M = metal which in this case could be only Na).

The results of the analyses of three runs which Xray methods had shown consisted of the same single phase are shown in Table III. As the high $GeO_2/$ Na₂O ratio was noted in several analyses, a series of quantitative reactions was run using 1:4 Na₂O-GeO₂ mixtures at 200° and with increasing time of reaction in order to determine the ratio at equilibrium. The progress of the reaction was followed by optical, infrared and X-ray analyses of the solid products, and by colorimetric analysis of the solutions. After 2 hours the solid product was found to contain roughly equal amounts of sodium tetragermanate and the hexagonal crystalline modification (soluble form) of germanium dioxide with a lesser amount of sodium hydrogen germanate. At this stage the crystals of the tetragermanate could be seen forming in and on the larger glassy hydrogen germanate crystals. A trace only of germanium dioxide remained after 12 hours and only a small amount of hydrogen germanate completely surrounded by tetragermanate crystals was detected. After 24 hours at 200° only the tetragermanate could be detected by X-ray analysis.

Table III

ANALYSIS OF RUNS WHICH BY X-RAY ANALYSIS CONTAIN A

	SINGLE	PHASE		
Crystal	Na₂O, %	GeO2, %	H₂O, %	Molar ratio GeO2/Na2O
Octagonal prism	11.5	85.5	0.33	4.42
Rectangular prism	12.6	85.3	. 50	4.01
Dipyramidal	12.2	87.5	.51	4.25
Calcd. Na2Ge4O9	12.9	87.1		4.00

The molar ratio of GeO₂/Na₂O in the solid product came to equilibrium at 4.3-4.5 and in the solution at 1.2-1.4. The average pH rose from 11.65 for the two hour runs to a maximum of 11.85 for the 12-hour runs, then fell to 11.55 after 24 hours with little further variation regardless of the reaction time. A check run which was allowed to stand 30 days before raising to temperature had a final pH of 10.48 for a 2-hour run and no germanium dioxide remained in the product, only tetragermanate. This give some indication of the reason for the variation of the results reported in Tables I and II from those of the series of runs just above.

After two months standing a precipitate formed in the hydrothermal run solutions having a $GeO_2/$ Na₂O ratio greater than 1.2. The ratio dropped to 1.0 with a corresponding average drop of 0.4 unit in pH. According to X-ray analysis the precipitate now contained a mixture of two MH3- Ge_2O_5 , one with too large a lattice constant to be $NaH_3Ge_2O_6$. This same X-ray pattern with double peaks was obtained for the solid product of a 110° run as shown in Table II, for the precipitate formed when a sodium hydroxide solution of germanium dioxide was saturated with sodium chloride, and for the product of a run in which an attempt had been made to prepare the tetragermanate hydrothermally at 200° from sodium metagermanate.6 As the infrared patterns indicate no new crystalline forms present, and also since the acid germanates are known to be zeolitic,6 the slight variation in patterns is at present attributed to two definite states of hydration.

Crystals of the tetragermanate with 5 ml. of water reacted at 200° for 2 days. There was no visible change in the crystals and the $\text{GeO}_2/\text{Na}_2\text{O}$ ratio in the solution was 1.0 and the pH 11.5. A run of 30 days under the same conditions resulted in the unusual combination of 10 mg. Na₂O/100 ml. with 860 mg. $\text{GeO}_2/100$ ml. (pH 10.7) in the liquid phase. The solid product contained only tetragermanate.

Attempts to prepare the tetragermanate hydrothermally at 200° from the metagermanate⁶ resulted in only the acid germanate. From a run which leaked dry slowly, long birefringent needles with indices $N_0 = 1.58-1.59$, $N_E 1.59-1.60$, presumably Na₂GeO₃ (anhyd.)^{1b} were obtained. From another run which leaked to 1 ml., crystals of index 1.50, presumably hydrated sodium metagermanate, was the only solid phase obtained.

For aid in spectral identification, since only the XRD pattern for NH₄H₃Ge₂O₆ appears in the A. S. T. M. Card File, some of the ammonium compound was prepared hydrothermally at 200° using a NH4OH-GeO2 mixture. It was confirmed⁶ that the X-ray pattern very closely resembled that for the corresponding sodium compound; however their infrared patterns had distinct differences. The sodium compound gave very strong absorption bands at 3.10 and 6.1 μ (water), and at 13.0 μ ; while the ammonium compound gave similarly strong bands at 3.15–3.20 and 7.10 μ (NH₄) and at 12.75 μ . A small shoulder only was visible at 3.00–3.05 on the first strong ammonium band and a small broad band at 6.1 that would indicate a small amount of water present either as hydrate water or molecular water. The infrared pattern for the potassium hydrogen germanate also showed by a weak band at $3.05 \ \mu$ only a small amount of water present, but had the same strong broad band at $13.0 \ \mu$ found in the corresponding sodium compound.

(15) "Handbook of Chemistry and Physics," 37th Ed., Chemical Rubber Pub. Co., Cleveland, Obio, reports 1.59.

Runs at 300° using the NH₄OH–GeO₂ mixture produced only the insoluble form of GeO₂. With GeO₂ glass present and runs at 200° a lower pH resulted, but with no visible effect on the formation of ammonium germanate. The glass was converted *in situ* to the soluble form in 1 day with a resulting pH of 9.95; while in 19 days the glass was converted to the insoluble form (pH 10.8).

Discussion

Since DTA analysis⁷ and infrared analysis show that the hydrated condensed germanate contains molecular water, as well as water of hydration, the formula Na₃HGe₇O₁₆·4H₂O will be used here in preference to Na₂Ge₅O₁₁. The former is also preferable to the general formula NaH₃Ge₂O₆⁶ since conversion of the hydrogen germanate to the tetragermanate by ignition also produced enough GeO₂ to be detected by X-ray and infrared analysis. This confirmed equation 1 as proposed by Nowotny $2Na_3HGe_7O_{16}\cdot4H_2O$

$$3Na_2Ge_4O_9 + 9H_2O + 2GeO_2$$
 (1)

and Wittmann,⁴ except no evidence was found that an equilibrium is reached, at least when the conversion is at high temperatures.

The ease of precipitation of polymeric germanates from basic GeO_2 solutions is said to indicate that polymeric germanate ions are present in solution.¹⁶ The slight acidity of aqueous GeO_2 solutions also has been attributed to an equilibrium similar to equation 2 which is displaced well to the

$$H_4GeO_4 \longrightarrow (HGe_7O_{16})^{3-} + 12H_2O + 3H^+ (2)$$

left.⁹ A rise in ρ H should increase the contribution of the polymeric ion. The fact that the NaOH-GeO₂ mixture of Table I at ρ H 7.8 became gelatinous after several months standing confirms this.

Potentiometric titration of a 0.048 M GeO₂ solution by 0.2 N NaOH resulted in a curve¹⁷ with a readily determined end-point at pH 10.75 and at a GeO₂/Na₂O ratio of 1.97. From this it is apparent that at the end-point the major germanate ion is $(H_3GeO_4)^-$ with a small contribution from $(H_2-GeO_4)^{2-}$. Since the polymeric germanate can be precipitated from solutions at this pH merely by adding NaCl there is undoubtedly some polymeric germanate present according to equation 3. Any decrease in pH should increase the amount.

$$7(H_3GeO_4) \xrightarrow{-} (HGe_7O_{16})^{3-} \xrightarrow{+} 8H_2O + 4OH^{-} (3)$$

The first step in hydrothermal reaction of NaOH-GeO₂ mixtures is the conversion of any excess polymeric germanate (gelatinous or otherwise) to crystalline form probably by removal of water. Since this does not disturb the small amount of hydrogen germanate in equilibrium in equations 2 and 3 the ρ H does not change. However, in longer runs in which the insoluble tetragermanate is formed, $(HGe_7O_{16})^{3-}$ ions are removed from the equilibrium. As is seen from Table II the ρ H then rises two ρ H units. It is evident from the final ρ H of 11.5–12.0 and solution ratio GeO₂/Na₂O = 1 that the major ion in solution after the run is (H₂-GeO₄).²⁻⁻

(16) P. Souchay, Bull. soc. chim., France, 395 (1953).

(17) Identical curves to those of Carpeni, *ibid.*, 1010 (1952), for KOH titrations of GeO₂ were obtained for NaOH.

The pH of the solutions in Table I does not change when the tetragermanate is formed. As can be seen from equation 3 the concentration of $(H_3GeO_4)^-$ would be small at this pH. Removal of $(HGe_7O_{16})^{3-}$ from the equilibrium then would produce little shift to the right and a corresponding rise in pH. Also the small amount of GeO₂ produced according to equation 1 would be of much greater importance.

There was no evidence of $(Ge_4O_9)^{2-}$ ions in solution. The precipitate from the run solutions contained a very small amount of birefringent material which could not be the acid germanate. Infrared and X-ray analyses indicated another compound present in small amount; however, it was unidentifiable with known patterns.

Since both the hydrogen germanates and tetragermanates prepared showed no noticeable tendency to absorb moisture from the air it is presumed that the hygroscopic product described by Nowotny and Wittmann⁵ contained residual metagermanate.

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[CONTRIBUTION FROM THE DEPARTMENT OF CHEMISTRY, CLARKSON COLLEGE OF TECHNOLOGY]

The Molecular Weight of the Phosphotungstic Acids by Light Scattering¹

By Milton Kerker, Dorothy Lee and Adam Chou Received September 3, 1957

The light scattering of 12-phosphotungstic and 9-phosphotungstic acids in a number of organic solvents and water has been determined. In the organic solvents, the molecular weight calculated for the former corresponds to the monomer, $H_3PW_{12}O_{40}$, while that of the latter corresponds to the dimer, $H_8P_2W_{18}O_{82}$. This is consistent with crystal structure studies by X-rays. The usual treatment is not adequate to interpret the data from aqueous solutions where these acids are strong.

Since the discovery of ammonium phosphomolybdate by Berzelius in 1826, the heteropoly acids and their salts have provided a fruitful testing ground for the theories of structural inorganic chemistry. The bewildering variety of species proposed in the literature and the lack of a critical evaluation of the great amount of experimental work at the turn of the century has necessitated a new look with the aid of modern structural tools.²

The best characterized of the phosphotungstic acids are those with empirical formulas H_3PW_{12} - O_{40} and $H_3PW_9O_{31}$, 12-phosphotungstic acid and 9phosphotungstic acid. The complete structure for these in the solid state has been elucidated by Keggin³ and Dawson.⁴ Dawson found that the unit cell of 9-phosphotungstic acid consists of the dimeric ion $P_2W_{18}O_{62}$ ⁻⁶. This agrees with the find-

(1) Supported in part by U. S. Atomic Energy Commission Contract Number AT(30-1)-1801.

(2) The standard treatises such as J. W. Mellor, "A Comprehensive Treatise on Inorganic and Theoretical Chemistry," Longmans, Green and Co., London, 1927-1937; J. Newton Friend, "Textbook of Inorganic Chemistry," Charles Griffin and Company, London, 1924-1930; and "Gmelins Handbuch der Anorganische Chemie," Verlag Chemie, Berlin, from 1926, summatize the literature to the early 1930's. The structural problem is stated in modern terms in such textbooks as W. Hückel, "Structural Chemistry of Inorganic Compounds," by Elsevier, New York, N. Y., 1950, p. 179; H. B. Jonassen in Bailar's "Chemistry of the Coördination Compounds," Reinhold Publ. Corp., New York, N. Y., 1956, Chapter 14; and A. F. Wells, "Structural Inorganic Chemistry." Oxford, 1950, p. 348. For present directions in research in this field see the preprints of papers read at the National Meeting of the A.C.S., Division of Physical and Inorganic Chemistry, Atlantic City, N. J., September 17, 1956.

at the National Meeting of the A.C.S., Division of Physical and Inorganic Chemistry, Atlantic City, N. J., September 17, 1956.
(3) J. F. Keggin, Nature, 131, 908 (1933); 132, 351 (1933); Proc. Roy. Soc. (London), A144, 75 (1934); J. W. Illingworth and J. F. Keggin, J. Chem. Soc., 575 (1935); A. J. Bradley and J. W. Illingworth, Proc. Roy. Soc. (London), A157, 113 (1936).

(4) B. Dawson, Acta Cryst., 6, 113 (1953).

ing of Souchay⁵ who proposed, on the basis of cryoscopy of the sodium salt in sodium sulfate at its transition point, that 9-phosphotungstic acid is the dimer, $H_6P_2W_{18}O_{62}$, whereas 12-phosphotungstic acid is monomeric, $H_3PW_{12}O_{40}$.

Although the structure of these acids in the solid state has been well established, the state of molecular aggregation in solution is hardly known. This knowledge constitutes the starting point for an understanding of the various aggregation, degradation and equilibrium phenomena encountered in solution. It is the purpose of this work to investigate the molecular weight of the 12- and 9-phosphotungstic acids in solution by means of light scattering in order to determine whether these species consist of monomers, dimers or higher polymers.

Experimental

Preparation and Analysis of Compounds. 1. 12-Phosphotungstic Acid.—The reagent grade chemical, commercially available from J. T. Baker Company, was used. The purity was checked by analysis of P_2O_5 and H_2O content, assuming the difference was WO_3 . After conversion to the Na salt by Na₂CO₅ fusion, the usual method of precipitation of phosphate with magnesia reagent and ignition to the pyrophosphate was used. The loss in weight at 600° was assumed to correspond to the water content. The W/P ratio was found to be 11.7 \pm 0.1. Considering the errors resulting from possible coprecipitation of WO₃ with the phosphate and the volatilization of P₂O₅ above 250°, the above accuracy was considered satisfactory.

above accuracy was considered satisfactory. 2. 9-Phosphotungstic Acid.—The method of Souchay⁶ which is a modification of that first reported by Wu^7 was used. One hundred g. of Na₂WO₄ was dissolved in 350 ml. of hot water and brought to a boil. One hundred and fifty ml. of 85% H₃PO₄ was added slowly to the boiling solution and the whole mixture was refluxed for 5 hr. or overnight

(6) P. Souchay, Bull. soc. chim., 365 (1951).

⁽⁵⁾ P. Souchay, Ann. Chim., [12] 2, 203 (1947).

⁽⁷⁾ H. Wu, J. Biol. Chem., 43, 189 (1920).